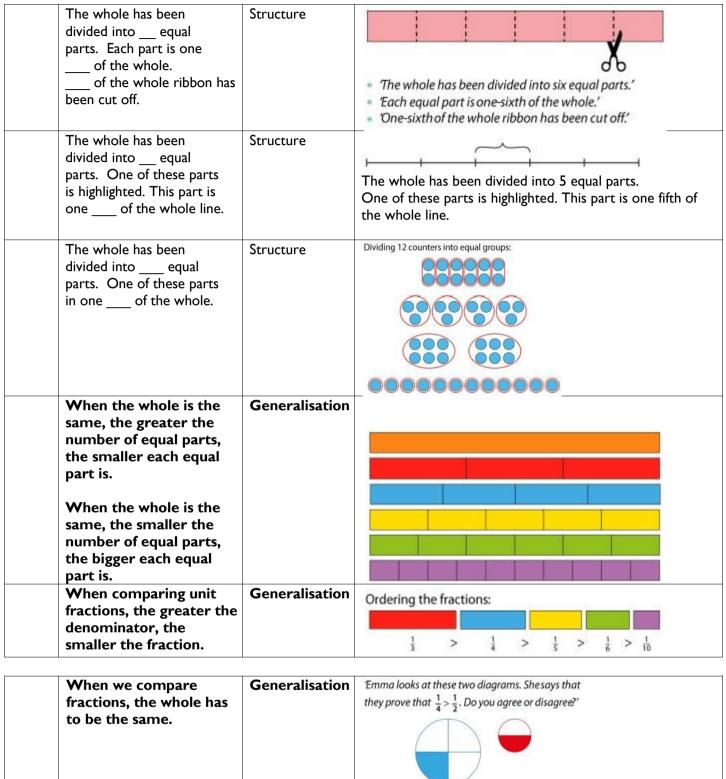


	Part-W	hole relationships
Example of stem	Type of stem	·
If is the whole then is part of the whole.	Structure	If Europe is the whole , then the United Kingdom is part of the whole. Mon Tue Wed Thu Fri Sat Sun
		Mon rue wed ma m sat san
		If the week is the while then Tuesday is part of the whole
A part is always smaller than the whole.	Generalisation	
If is the whole then is not part of the whole.	Structure	If my face is the whole then my foot is not part of the whole.
The whole has been divided into equal / unequal parts.	Structure / language	
The whole has been divided into equal parts.	Structure	The whole has been divided into 4 equal parts.
The parts are equal , I know this because the number of in each part is the same.	Structure	
The parts are unequal , I know this because the number of in each part is not the same .	Structure / language	



Different parts of the samesized whole can be directly compared based on their size. As the while increases in size and the size of the selected part remains the same, each part becomes smaller in relation to the whole.	Generalisation Generalisation	In the first set of counters, the yel smaller part of the whole then in the smaller part of the whole the wh	
	11	nit Fractions	70/8
A unit fraction is any fraction where the numerator is one.	Generalisation	Numerator (1 for a unit fractions One of the parts of the whole Denominator The number of equal parts the whole	ole
The whole has been divided into equal parts of the parts has been shaded.	Structure / language	The whole has been divided into the parts has been shaded.	hree equal parts. One pf
	Language /	Say	Write
	structure	'The whole has been divided'	COURT TO DESCRIPTION AND
			The division bar:-
		'into 3 equal parts.'	The denominator: 3
		'One of the parts has been shaded.'	The numerator: 1
The denominator is because the whole is divided into equal parts. The numerator is one because one part is shaded.	Structure	The denominaor is 4 because the equal parts. The numerator is I because one parts.	

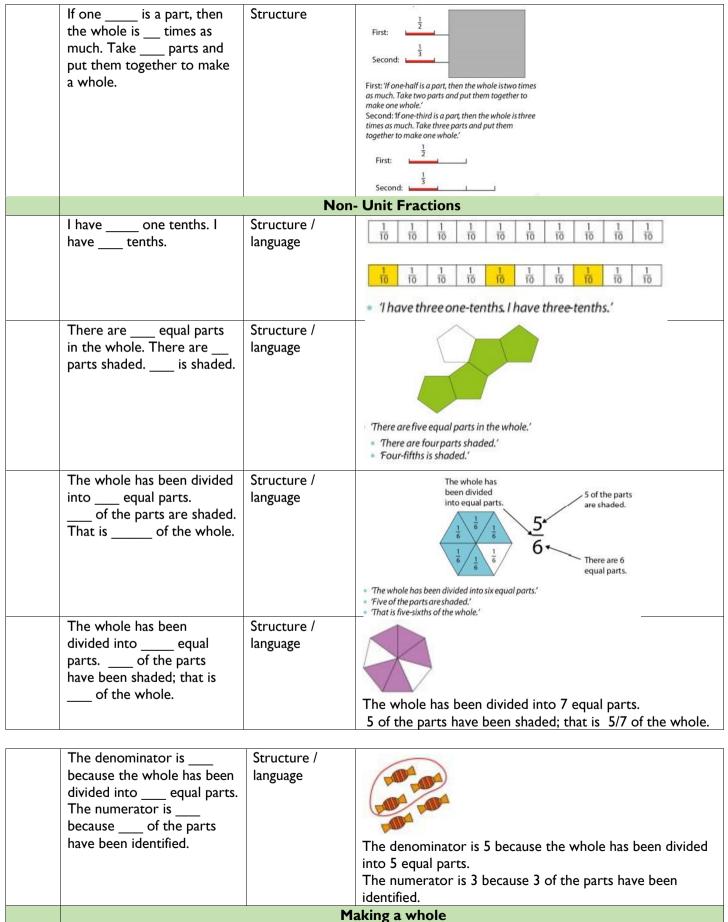




'Disagree: to compare fractions, the wholes must

the same."







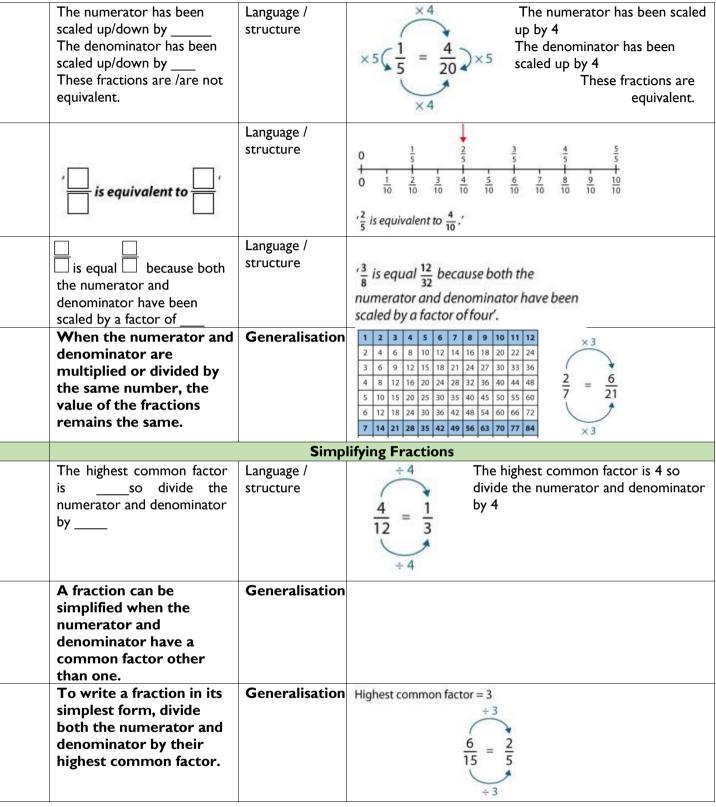
When the numerator and the denominator are the same the fraction is equivalent to one whole.	Generalisation		\$\frac{5}{5}\$	$\frac{5}{5} = 1$	$\frac{9}{9} = 1$ $\frac{11}{11}$	$\frac{2}{2} = 1$
		0 1/5	2 3 4 5	555	rea cm	
		5 one-fifths 0 1/5 2/5	3 4 5	1		
If we know the size of a unit fraction, we can work out the size of the whole.	Generalisation	Part	Part as a fraction of the whole	Number of equal parts in the whole	Whole	
			<u>1</u> 5	5		
Divide by the numerator to find one part. Multiply the denominator to find the whole.	Generalisation	$\frac{1}{3}$ of the n	umber is 8.' umber is 4.' umber is 12.'		8 ÷ 2 = 4 4 × 3 = 12	
	Counting in	fractional	steps			
The line is divided into equal parts. This allows us to count in	Structure		-	1		
		0 1/4		' 		
The interval is divided into equal parts. This allows us to count in	Structure		us to count in g	3 1 1 divided into fou uarters'		
		1 1 0	+++++	 	2 2 2 3 +++ 3	
	nproper fractions	and mixe	ed numbers			
Quantities made up of both whole numbers and a fractional part can be expressed as mixed numbers.	Generalisation	2	$\frac{1}{2}$			



Each whole is divided into four equal parts. We have of these equal parts. This represents quarter(s)	Structure/ language		is divided into four equ parts. This represents		
The denominator is This means that each whole has been split into equal parts parts make each whole. The numerator is This means there are equal parts. It is possible to make full groups of quarters and there are more quarters.	Structure/ language	The denomi been split in The numera	inator is 4. This means to 4 equal parts. 4 part ator is 10. This means to to make 2 full groups quarters	s make ead here are 10	h whole.) equal parts.
Our unit is so we will be thinking about groups of There are in one whole.	Structure / language	Our unit is eighth groups of eight.' There are \$\frac{8}{8}\$ in one	21 8 s s o we will be thinking about		
How many groups of —in — groups and more	Structure / language	Improper fraction	Prompt question How many groups of 10/10 in 21/10? (2 groups and 1 more tenth.)	Mixed number	
There are groups of sixths which is sixths and more sixths, so that is sixths	Structure / language	$3\frac{1}{6} = \frac{\Box}{6}$	There are three groups of $\frac{6}{6}$ which is $\frac{1}{6}$ which is $\frac{1}$	th is $\frac{18}{6}$, and one	more sixth; that's $\frac{19}{6}$
		1 + + + +	6 12 6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	18 6 1 3	$\begin{array}{c c} & \frac{24}{6} \\ 3\frac{1}{6} & 4 \end{array}$

	Equiv	alent Fi	ractions		
When two or more fractions have the same value. We call them equivalent fractions.	Generalisation		<u>8</u> 24	← ¹ / ₃	<u>←</u> 3/9







is not in its simplest form because is a common factor of and is in its simplest form because one is the only common factor of and	Language / structure.	'Sort the following numbers according to whether they are expressed in their simplest form or not.' $\frac{3}{15} \frac{2}{5} \frac{4}{20} \frac{25}{36} \frac{1}{6} \frac{7}{21} \frac{18}{30} \frac{9}{17}$ $\frac{5}{15} \frac{11}{20} \frac{23}{30}$ A/20 is not in its simplest form because four is a common factor of 4 and 20 $23/50 \text{ is in its simplest form because one is the only common factor of 23 and 30.}$
	Comp	paring Fractions
islot of	Language / structure	$\frac{1}{4} < \frac{3}{4}$ $\frac{1}{4}$ is I lots of $\frac{1}{4}$ $\frac{3}{4}$ is 3 lots fo $\frac{1}{4}$ I know that I is less than 3 so $\frac{1}{4}$ is less than $\frac{3}{4}$.
When we compare fractions with the same denominator, the greater the numerator, the greater the fraction.	Generalisation	$ \frac{18}{24} \frac{23}{24} $ $ \frac{18}{24} \frac{23}{24} $ $ \frac{18}{24} \frac{23}{24} $ $ \frac{18}{24} \frac{23}{24} $ $ \frac{18}{24} 23 \text{ lots of } \frac{1}{24} $ $ \frac{18}{24} < \frac{23}{24} $
When comparing unit fractions, the greater the denominator the smaller the fraction.	Generalisation	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
When we compare fractions with the same numerator, the greater the denominator, the smaller the fraction.	Generalisation	$\frac{2}{10} > \frac{2}{12} \qquad 1$
To compare fractions with different numerators and denominator convert to common denominators.	Generalisation	$\begin{array}{cccc} \frac{1}{3} & & & \frac{3}{4} \\ \downarrow & & & \downarrow \\ \frac{4}{12} & & & \frac{9}{12} \end{array}$



islot of 1	Language / structure	$\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$
tenths and more tenths make tenths.	Structure	$\frac{1}{5} + \frac{1}{5} + \frac{1}{5} = \frac{3}{5}$ $\frac{3}{5} = \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$ 3/5 is 3 lots of 1/5. $\frac{\frac{6}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{1}{10}} = \frac{\frac{2}{10}}{\frac{2}{10}} = \frac{2}{10}$
		$0 \frac{1}{10} \frac{2}{10} \frac{3}{10} \frac{4}{10} \frac{5}{10} \frac{6}{10} \frac{7}{10} \frac{8}{10} \frac{9}{10} 1$
·	Structure	6 tenths and 2 more tenths make 8 tenths.
islots of' islots of' islots of' 'I know that + =' 'so, I know that + ='	Structure	' $\frac{6}{10}$ is six lots of $\frac{1}{10}$.' ' $\frac{2}{10}$ is two lots of $\frac{1}{10}$.' 'I know that $6 + 2 = 8$.' 'so, I know that $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$.'
When adding fractions	Generalisation	
with the same denominators, just add the numerators.		
/10 is lots of I/10 /10 is lots of I/10 I know that = = So I know that/10/10 =/10	Structure	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
When subtracting	Generalisation	W N 100
fractions with the same denominators, just subtract the numerators.		$\frac{8}{9} - \frac{3}{9} = \frac{5}{9}$ $\frac{8}{10} - \frac{2}{10} = \frac{6}{10}$
To subtract from one whole, first convert the whole to a fraction where the denominator and numerator are the same.	Generalisation	'A watermelon is cut into 8 equal pieces.' '\frac{6}{8} \text{ of the watermelon is eaten'} What fraction of the watermelon is left?' Eaten: $\frac{6}{8}$ Left: $\frac{2}{8}$ $\frac{8}{8} - \frac{6}{8} = \frac{2}{8}$



The parts are and The total or whole is	Language / structure.	QQ
		$\left(\begin{array}{cccc} \frac{2}{5} \end{array}\right) \left(\begin{array}{cccc} \frac{1}{5} \end{array}\right) \left(\begin{array}{ccccc} \frac{1}{5} \end{array}\right) \left(\begin{array}{ccccc} \frac{2}{5} \end{array}\right)$
		+ 2/5
		11/5
		The parts are $\frac{2}{5}$ and $1\frac{1}{5}$. The total, or whole, is $1\frac{3}{5}$.
Related fractions have denominators where one denominator is a multiple of the other.	Generalisation	1/3 and 1/9
		We can change $\frac{1}{3}$ to $\frac{3}{9}$.'
and are realted	Structure / language	
denominator is a multiple of the other denominator		$^{\prime}\frac{1}{16}$ and $\frac{1}{4}$ are related fractions because the denominator, "16", is a multiple of the other denominator, "4".
Fractions must have the same denominator before	Generalisation	$\frac{1}{4} + \frac{1}{4} = \frac{2}{4}$
they can be added or subtracted.		
When fractions have the same denominator, we call this a common denominator.	Generalisation	
To add or subtract fractions with different denominators, first convert to fractions with	Generalisation	$\frac{24}{36} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6}$ $= \frac{2+1}{6} = \frac{31}{62} = \frac{1}{2}$
a common denominator.		$=\frac{1}{6}$
		To solve 1/3 + 1/6, convert 1/3 to 2/6 by scaling 1
		and 3 up by two then add 2/6 and 1/6 together.
To find a common denominator, identify the	Generalisation	$\frac{1}{3} + \frac{1}{5} = \frac{5}{15} + \frac{3}{15}$
lowest common multiple		
of the denominators then create an equivalent		Multiples of 2: 2: 6: 0. 12: 15
fraction.		Multiples of 3: 3, 6, 9, 12, <mark>15</mark> Multiples of 5: 5, 10, <mark>15</mark>
We can find a common	Generalisation	The lowest common multiple of 3 and 5 is 15. $\frac{1}{3} + \frac{1}{5} = \frac{5}{15} + \frac{3}{15}$
denominator for two nonrelated fractions by multiplying their denominators.		
40.10111114C013.		If you multiply the two denominators 3 and 5 you will get the common denominator product of 15.



Mu	Itiplying whole n	numbers and fractions
The whole has been divided into equal parts, and one of these parts is	Structure	$\frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9} \frac{1}{9}$ $\frac{1}{9} + \frac{1}{9} = 9 \times \frac{1}{9}$ • The whole has been divided into nine equal parts, and one of these parts is $\frac{1}{9}$.'
lot(s) of is equal to	Structure / language	
To multiply a fraction and a whole number, we multiply the numerator by the whole number and keep the denominator the same.		
lots of is equal to lots of	Structure	Commutativity: $3 \times \frac{4}{5} = \frac{12}{5} = 2\frac{2}{5}$ $\frac{4}{5} \times 3 = \frac{12}{5} = 2\frac{2}{5}$ $3 \times 4/5 = 4/5 \times 3$
Each part is of the whole; of is is divided into equal parts;	Structure / language	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
of = lots of =	Structure / language	$0 = 10$ $y = 5$ $\frac{1}{2} \text{ of } 10 = 5'$ $2 \text{ lots of } 5 = 10.'$
When a whole number is multiplied by a unit fraction, it makes the whole number smaller	Generalisation	



To calculate a fraction of	Generalisation	Calculate $\frac{3}{5}$ of 15
a quantity, find the unit		15
fraction of the quantity.		15
Then multiply the unit		3 3 3 3
fraction by the		
numerator.		$\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$
		Find the unit fraction $(\frac{1}{5})$ of 15 by dividing
		15 into five equal parts. $\frac{1}{5}$ of 15 is 3 so $\frac{3}{5}$
		of 15 is 9.
When a whole number is	Generalisation	
multiplied by a proper		
fraction, it makes the		
whole number smaller		
There wereequal parts	Language /	1
in the whole. Each of the	structure	1 1 1
three parts was halved so we		3 3 3
now have equal parts in		6 6 6 6
the whole.		There were 3 equal parts in the whole. Each of the three
		parts was halved so we now have six equal parts in the
		whole.
When multiplying unit	Generalisation	1 1 1 1 1 1
fractions, multiply the		$\frac{1}{2} \times \frac{1}{6} = \frac{1}{12}$ $\frac{1}{6} \times \frac{1}{2} = \frac{1}{12}$
denominators.		
		$\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$ $\frac{1}{5} \times \frac{1}{3} = \frac{1}{15}$
		0.5 C.0.6 VII.D. C.4 VII. 11.
When multiplying unto	Generalisation	
fractions, the product is		
smaller than the fractions		
being multiplied		
To multiply fractions, we	Generalisation	
can multiply the		4 2 8
numerators ad multiply		-X-=-
the denominators.		5 3 15
	Dividing	g fractions
To divide a fraction by a	Structure	1
whole number, we can		$\frac{1}{2}$ $\frac{1}{3}$ $\frac{1}{3}$
change it to an equivalent		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
multiplication. To divide by		
, we can multiply by		$\frac{1}{3} \div 5 = \frac{1}{15} \longrightarrow \frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$
		'To divide a fraction by a whole number, we can
		change it to an equivalent multiplication. To divide by
		five, we can multiply by $\frac{1}{5}$.
		11ve, we cult multiply by 5.
To divide a fraction by a	Generalisation	
whole number, we can		
change it to an equivalent		
multiplication.		



To divide by we can multiply by	Structure	$\frac{1}{3} \div 4 = \frac{1}{12}$ $\frac{1}{3} \times \frac{1}{4} = \frac{1}{12}$
		$\frac{1}{3} \times \frac{1}{4} = \frac{1}{12}$
If we divide into equal groups, then each of the groups is because ÷	Structure	$\frac{6}{7} \div 3 \begin{array}{ c c c c c c c c c c c c c c c c c c c$
=		If we divide six 1/7 into 3 equal groups, then each of the groups os 2/7 because $6 \div 3 = 2$
If the divisor is a factor of the numerator, just divide the numerator by	Generalisation	$\frac{8}{10} - 4 = \frac{2}{10}$
the denominator and keep the denominator		10
the same.	ing fractions do	cimals and percentages
	Generalisation	-
In order to use a place value chart to help convert a fraction to a decimal, the fraction must be expressed as a tenth, hundredth or thousandth.	Generalisation	$\frac{\frac{1}{5} = \frac{2}{10}}{\text{ones}} \text{ tenths}$
A fraction can be	Generalisation	
converted into a decimal	. Generalisation	0 · 2
by dividing the numerator		$\frac{1}{2} = 5 \frac{0.2}{1.0}$
by the denominator.		5 - 3 11 0
·, is equivalent to	Structure	
We know that		'0.6 is equivalent to $\frac{3}{5}$.' 'We know that $\frac{3}{5} < \frac{4}{5}$, so $0.6 < \frac{4}{5}$.'
<		$0.6 \leqslant \frac{4}{5} \checkmark$
or ' is equivalent to '		$0.6 = \frac{3}{5}$
'We know that, <,		3
so<'.		$\frac{3}{5}$ < $\frac{4}{5}$
In order to convert a percentages to a fraction, first convert it to a fraction with a denominator of 100 then simplify.	Generalisation	$45\% = \frac{1}{100} = \frac{1}{20} \qquad 12\% = \frac{12}{100} = \frac{3}{25}$
To find 50% of a number, halve it.	Generalisation	'Zara is doing a 420 km charity bike ride. So far, she has completed 50% of the route. How far has she cycled?' 50% 0% 100%
		0km 420km
		1000 (1000)
		• '100% of 420 km is 420 km.'
		• '50% of 420 km is \frac{1}{2} of 420 km.' • 'Zara has cycled 210 km'



To find 10% of a number, divide it by ten.	Generalisation	Rishi has completed 10% of the same bike ride. How far has he cycled?' 10% 0% 透 100% +
		 '100% of 420 km is 420 km.' '10% of 420 km is ¹/₁₀ of 420 km.' 'Rishi has cycled 42 km.'
To find 1% of a number, divide it by hundred.	Generalisation .	'100% of 420 km is 420 km.' '1% of 420 km is $\frac{1}{100}$ of 420 km.' 'James has cycled 4.2 km.'